

Lamb Meat Quality Assessment by Support Vector Machines[†]

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Abstract. The correct assessment of meat quality (i.e., to fulfill the consumer's needs) is crucial element within the meat industry. Although there are several factors that affect the perception of taste, *tenderness* is considered the most important characteristic. In this paper, a *Feature Selection* procedure, based on a *Sensitivity Analysis*, is combined with a *Support Vector Machine*, in order to predict lamb meat tenderness. This real-world problem is defined in terms of two difficult regression tasks, by modeling objective (e.g. *Warner-Bratzler Shear* force) and subjective (e.g. human taste panel) measurements. In both cases, the proposed solution is competitive when compared with other neural (e.g. *Multilayer Perceptron*) and *Multiple Regression* approaches.

Keywords: Regression; Multilayer Perceptrons; Support Vector Machines; Meat Quality; Data Mining; Feature Selection

1. Introduction

A top priority factor in the success of meat industry relies on the ability to deliver specialties that satisfy the consumer's taste requirements. In particular, assessing the quality of an item is important for lamb meat firms, specially if they want to move into niche markets by differentiating their products. Therefore, meat and animal scientists have dedicated high efforts in finding reliable quality estimators. Among the several factors that influence meat quality (e.g. *juiciness*, *appearance* or *aroma*), *tenderness* is considered the most important attribute [11]. In effect, consumers are willing to pay premium prices for tender meat.

The ideal method for measuring tenderness should be accurate, fast, automated and noninvasive. In the past, two major approaches have been proposed [1]: *instrumental* and *sensory* analysis. The former is based in an objective test, such as the *Instron* instrument, which measures the *Warner-Bratzler Shear (WBS)* force and it is the most commonly used device. On the other hand, sensory methods are based

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in subjective information, usually given by a human taste panel. Both approaches are invasive, expensive and time demanding, since they require laboratory work. For instance, the *WBS* values can only be obtained 72 hours after slaughtering, while the preparation and execution of consumer taste panel may take several days.

An alternative is to use cheap and non invasive carcass measurements that can be collected within the first 24 hours after slaughtering (e.g. pH and color). Under this scenario, the classic animal science approach is based on *Multiple Regression* models [1], using meat features as independent (or input) variables and the *WBS* or *sensory* measures as the depended (or output) ones. However, the linear models will fail when nonlinear relationships are present. In such cases, a better option is to use techniques such as *Neural Networks (NNs)* [9] or *Support Vector Machines (SVMs)* [20]. Indeed, these methods are gaining an attention within the *Data Mining* field, due to their performance in terms of predictive knowledge [16][8]. It should be stressed that *SVMs* present theoretical advantages over *NNs*, such as the absence of local minima in the model optimization phase.

In *Data Mining* applications, besides obtaining a high predictive performance, it is often useful to provide explanatory knowledge. In particular, the measure of input importance is relevant within this domain. Since carcass features are often highly correlated, *Principal Component Analysis* has been proposed to reduce the input dimensionality [1]. Yet, the principal components are compressed variables and they do not represent a direct meaning for the meat user. An alternative, is to use a *Sensitivity Analysis* procedure, which has outperformed other input selection techniques (e.g. *Forward Selection* and *Genetic Algorithms*) [12].

In the last few years, several authors have proposed nonlinear methods to assess meat quality (e.g. beef, pork, poultry or sausages) [1]. In the majority of these studies, the *Multilayer Perceptron* neural architecture is the most common approach. However, regarding tenderness prediction, the literature seems scarce and it is primarily oriented towards beef. For example, in the work of Li et al. [15], *Multilayer Perceptrons* outperformed a *Multiple Regression* when mapping beef texture images with sensory tenderness scores. In another study, Hill et al. [10] have applied *Multilayer Perceptrons* to predict the *Instron* force, obtaining better results than the *Multiple Regression* method. More recently, Diez et el. [6] adapted a *SVM* with a polynomial kernel of degree 2 to model beef tenderness preferences, surpassing linear and cubic regression methods.

In this work, the combination of a feature selection procedure, based on a *Sensitivity Analysis*, with a gaussian kernel *SVM* is proposed to

predict lamb meat tenderness. This real-world problem will be modeled in terms of two regression tasks, using both instrumental and sensory measurements. The devised strategy will be tested on animal data and compared with other *NN* and *Multiple Regression* approaches.

The paper is organized as follows. First, a description is given on the datasets used (Section 2.1). Then, the learning models are presented (Section 2.2). In Section 3, the experiments performed are described and the results analyzed. Finally, closing conclusions are drawn (Section 4).

2. Materials and Methods

2.1. LAMB MEAT DATA

This study considered lamb animals with the *Protected Designation of Origin* certificate, from the *Trás-os-Montes* northeast region of Portugal. The database was collected from November/2002 until November/2003, with each instance denoting the readings obtained from a slaughtered animal. With a total of 81 examples, the database is quite small. However, it should be noted that each animal presents considerable costs, around 6 euros per kilogram plus laboratory work. Table I presents a synopsis of the data attributes. The **HCW** is obtained one hour after slaughter, exfoliation and evisceration. The former two attributes (**Breed** and **Sex**) are also registered at slaughterhouse, while the others are measured in laboratory. Due to their visual nature, the color attributes (**a***, **b***, **dE**, **dL** and **dB***) have a high impact in consumer's perception. In most of the situations, these are the only attributes that the consumer can judge.

*** Insert Table I around here ***

The **WBS** force is the major index for measuring meat tenderness. It can only be obtained in laboratory, no sooner than 72 hours after slaughter, by using an invasive device called *Instron*. The **WBS** registers the force (in *kg*) required to crush a meat sample with a thickness of 1*cm*. Low values suggest tender meat while high readings suggest toughness. On the other hand, a more elaborated scheme was devised to obtain the sensory values (**STP**). A panel of 12 trained individuals, from the *Bragança Polytechnic Institute*, was selected. Then, meat samples from the *longissimus thoracis* muscle were collected and defrost at 4°C in a refrigerator. Next, each sample was randomly encoded with a 3 digit number, wrapped in an aluminum sheet and heated at 100°C. Then, each panel member was set in an individual compartment,

performing a taste proof, under similar conditions, of random selected samples. Between different tastes, mouths were cleaned by using water and by eating small golden apple pieces. Each sample was ranked from 0 (the most tender) to 10 (the most tough). Finally, the **STP** attribute was measured as the average of the grades from the panel.

Since the original data contained missing values (2 for the **WBS** and 10 for the **STP**), two new datasets were created by discarding these entries. The first contains 79 rows (for the **WBS** task), while the second has 71 examples (**STP**). Figure 1 shows the histograms of the target variables.

*** Insert Figure 1 around here ***

2.2. LEARNING MODELS

A regression dataset D is made up of $k \in \{1, \dots, N\}$ examples, each mapping an input vector (x_1^k, \dots, x_I^k) to a given target y_k . The error is given by: $e_k = y_k - \hat{y}_k$, where \hat{y}_k represents the predicted value for the k input pattern. The overall performance is computed by a global metric, namely the *Mean Absolute Deviation (MAD)* and *Relative Mean Absolute Deviation (RMAD)*, which can be computed as [6]:

$$\begin{aligned} MAD &= 1/N \times \sum_{i=1}^N |y_i - \hat{y}_i| \\ RMAD &= 1/N \times MAD / \sum_{i=1}^N |y_i - \bar{y}_i| \times 100 (\%) \end{aligned} \quad (1)$$

In both metrics, lower values result in better predictive models. The *RMAD* statistic is scale independent, where 100% denotes an error similar to the naive average predictor (\bar{y}).

The *Multiple Regression (MR)* model is defined by the equation [8]:

$$\hat{y} = w_0 + \sum_{i=1}^I w_i x_i \quad (2)$$

where (x_1, \dots, x_I) denotes the input vector and $\{w_0, \dots, w_I\}$ the parameters to be adjusted. This model is easy to interpret and has been widely used in regression applications.

This study will consider the *Multilayer Perceptron* [9], the most popular *Neural Network (NN)* architecture. The base network will use biases, one hidden layer of H hidden nodes and logistic activation functions and one output node with a linear function [8]. Thus, each regression task (**WBS** and **STP**) will be modeled by a different *NN*. The overall model is given by the equation:

$$\hat{y} = w_{o,0} + \sum_{j=I+1}^{o-1} f\left(\sum_{i=1}^I x_i w_{j,i} + w_{j,0}\right) w_{o,i} \quad (3)$$

where $w_{i,j}$ denotes the weight of the connection from node j to i , o the output node and f the logistic function ($\frac{1}{1+e^{-x}}$).

The *NN* performance will be sensitive to the topology choice. To solve this issue, a common practice is to use a large number of hidden nodes (H) and train the *NN* with a *regularization* method. Thus, a *weight decay* procedure will be adopted, where the hyperparameter λ will control the network complexity [8].

All attributes are standardized to a zero mean and one standard deviation. Then, the initial neural weights are randomly set within the range $[-0.7, +0.7]$. Next, the training algorithm is applied and stopped when the error slope approaches zero or after a maximum of E epochs. Since the *NN* cost function is nonconvex (with multiple minima), R runs will be applied to each neural configuration, being selected the *NN* with the lowest penalized error.

In *Support Vector Machine (SVM)* regression, the input $x \in \mathbb{R}^I$ is transformed into a high m -dimensional feature space, by using a nonlinear mapping. Then, the *SVM* finds the best linear separating hyperplane in the feature space:

$$\hat{y} = w_0 + \sum_{i=1}^m w_i \phi_i(x) \quad (4)$$

where $\phi_i(x)$ represents a nonlinear transformation, according to the kernel function $K(x, x') = \sum_{i=1}^m \phi_i(x) \phi_i(x')$.

To estimate the best *SVM*, the ϵ -insensitive loss function (Figure 2) is often used [18]. The *Radial Basis Function* kernel, which presents less hyperparameters and numerical difficulties than other kernels (e.g. polynomial or sigmoid), will also be adopted [4]:

$$K(x, x') = \exp(-\gamma \|x - x'\|^2), \quad \gamma > 0 \quad (5)$$

Under this setup, the performance is affected by three parameters: C , a trade-off between the model complexity and the amount up to which deviations larger than ϵ are tolerated; ϵ , the width of the ϵ -insensitive zone; and γ , the parameter of the kernel. Since the search space for the three parameters is high, the C and ϵ values will be set using the heuristics proposed in [5]:

$$\begin{aligned} C &= 3\sigma_y, \text{ if } \bar{y} = 0 \\ \hat{\sigma} &= 1.5/N \times \sum_{i=1}^N (y_i - \hat{y}_i)^2 \\ \epsilon &= \hat{\sigma}/\sqrt{N} \end{aligned} \quad (6)$$

where σ_y denotes the standard deviation of the output (y) and \hat{y} is the value predicted by the 3-nearest neighbor algorithm. Since all variables were standardized to a zero mean, the $\bar{y} = 0$ condition is met.

*** Insert Figure 2 around here ***

The hyperparameters (λ and γ) will be tuned by a two level grid-search. The first level will search the best value (λ_1 or γ_1) within the ranges $\lambda \in \{0.00, 0.01, \dots, 0.20\}$ or $\gamma \in \{2^{-15}, 2^{-13}, \dots, 2^3\}$, as advised in [8, 4]. The second level proceeds with a fine tune within the range $\lambda_2 \in \{\lambda_1 - 0.005, \dots, \lambda_1 - 0.001, \lambda_1 + 0.001, \dots, \lambda_1 + 0.004\} \wedge \lambda_2 \geq 0$ or $\gamma_2 \in \{2^{s_1-1.75}, \dots, 2^{s_1-0.25}, 2^{s_1+0.25}, \dots, 2^{s_1+1.25}\} \wedge \gamma_2 \geq 0$. The prediction accuracy (MAD) in the grid-search is estimated by adopting a 10-fold cross-validation [13]. After obtaining the best parameter, the final model is optimized using the whole training data.

2.3. FEATURE SELECTION

Nonlinear models such as *NNs* and *SVMs* are sensitive to the *curse of dimensionality* [8][2], i.e., the number of samples should grow exponentially as number of inputs increases. Hence, when small datasets are available, feature selection is expected to reduce the prediction error. Moreover, measurement requirements are reduced and simpler models, which are easier to interpret by the final user, are produced.

In this work, a *Sensitivity Analysis* procedure will be used to guide the feature selection search. The *Sensitivity Analysis* is performed after model estimation and it is measured by the variance (V_a) produced in the output (\hat{y}) when the input attribute (a) is moved through its entire range [12]:

$$\begin{aligned} V_a &= \sum_{i=1}^L (\hat{y}_i - \bar{\hat{y}}) / (L - 1) \\ R_a &= V_a / \sum_{j=1}^I V_j \times 100 (\%) \end{aligned} \quad (7)$$

where I denotes the number of input attributes and R_a the relative importance of the a attribute. The \hat{y}_i output is obtained by holding all input variables at their average values. The exception is x_a , which varies through its entire range with L levels.

The proposed feature selection will work as an iterative backward method, using all inputs at the beginning. In each iteration, a 10-fold cross-validation is performed over the training data. The intention is to get a robust estimation of the quality of the inputs. Thus, the input importance values (R_a) are averaged over the 10-fold trainings and the least important attribute (\bar{R}_{min}) is discarded. Due to the computational effort, only one hyperparameter, set to the middle of the first level search range ($\lambda = 0.1$ or $\gamma = 2^{-7}$), is tested during this phase. The algorithm is stopped after T iterations. Then, the second level cross-validation grid search is executed, in order to fine tune the hyperparameter. Finally, the best model is trained using the whole training data.

3. Results

All experiments were conducted with a *Pentium IV* processor, under the *Linux* operating system. The simulations were programmed in the **R** environment [17], an open source and high-level programming language that provides powerful tools for statistical analysis. The *NNs* were trained with the *BFGS* algorithm from the family of quasi-Newton methods, as implemented in the **R** *nnet* library. The **R** *kernlab* package was adopted for the *SVM* fitting, which uses the *Sequential Minimal Optimization* algorithm that is implemented by the *LIBSVM* tool [4].

After preliminary experiments, the maximum number of *NN* training epochs was set to $E = 10$. Further values increased the computational effort with no improvement in performance. The number of hidden nodes was fixed to $H = 12$ and the number of runs was set to $R = 3$. Regarding the *SVMs*, the tolerance of termination criterion was set to the default value (0.001). Finally, the sensitivity parameters were set to $L = 2$ for the binary attributes and $L = 5$ for the continuous inputs, while the termination criterion was set to $T = 6$. This last value was set after monitoring the validation error progress in some of the initial experiments.

In order to compare the learning models, 30 runs of a leave-one-out procedure [13] (computed over all available data) were executed (in a total of $30 \times N$ experiments). The results are shown in Table II, in terms of the average of the test errors, with the correspondent t-student 95% confidence intervals [7]. Column **Time** denotes the required computation for each method (in seconds).

*** Insert Table II around here ***

First, the analysis will be given for the models what use all twelve inputs. The *Multiple Regression (MR)* results are the worst for the **WBS** task. This scenario changes for the sensory panel, where the *MR* is the second best method, outperforming the *NN* method. Regarding the nonlinear methods, the *SVM* is the best method for both datasets, outperforming (with statistical significance) the *NN* and *MR* models. In addition, the computational effort also favors the *SVM*, since the *NN* demands a computational increase around a factor of 2.5. Overall, the *RMAD* values suggest that the second task is more difficult than the first one.

While only using half the inputs, the *Feature Selection (FS)* based approaches (*FSNN* and *FSSVM*) give rise to better/slightly better performances. In terms of the average *RMAD* values and for the **WBS** output, there is an improvement of 0.6% (not statistically significant)

for the *FSNN* and 2.0% (statistically significant) for the *FSSVM* model. Turning to the second task, the average *RMAD* decrease is 7.3% (statistically significant) for the *FSNN* and 0.2% (not statistically significant) for the *FSSVM*. In terms of the final comparison, *FSSVM* is the advised method, since it presents a lower mean and confidence interval values, when compared with the other models.

Table III shows the average relative importance (Equation 7) of the input variables for the best methods. To simplify the analysis, the less important attributes ($R_a \leq 1\%$) were removed from the table (**Sex**, **C** and **b***). It should also be noted that the table contains more than six attributes, since in each simulation different sets of features can be selected. The **Sex** attribute is the least relevant factor ($R_a \leq 0.1\%$), which contrasts with the knowledge that gender affects tenderness. Since female meat often present a higher weight and fatness, the sex information could be indirectly represented in the **HCW** and **STF2** variables. However, additional experiments where these attributes were replaced by the **Sex** input and the models retrained did not provide evidence for this claim.

*** Insert Table III around here ***

In general, the results are similar for both *NN* and *SVM* based methods. For the **WBS** task, the red color (**a***) is the highest important attribute. Turning to the **STP** problem, the most relevant features are the **Breed** and red index (**a***). The differences obtained between the two tasks may be explained by psychological factors. For instance, the **Breed** importance increased from 0.4/0.3% (**WBS**) to 35.3/41.3% (**STP**). This is a surprising result, since it contradicts the animal science theory.

As an example, the left of Figure 3 shows the scatter plots (predicted versus the observed values) for the **WBS** task. In the figure, the diagonal line denotes the perfect forecast. The *Regression Error Characteristic (REC)* curves [3] are also shown (right of the figure) for the *FSSVM*, *MR* and *Average Predictor* methods. The *REC* curve is used to compare regression models and it plots the error tolerance (x -axis), given in terms of the absolute deviation, versus the percentage of points predicted within the tolerance (y -axis). In the figure, the *FSSVM* line is above the other curves for the majority of the x values. Overall, it presents an higher area, denoting a better fit.

*** Insert Figure 3 around here ***

4. Conclusions

In this work, a *Feature Selection (FS)* procedure, based on a *Sensitivity Analysis*, is combined with a *Support Vector Machine (SVM)*, aiming at the prediction of lamb meat tenderness. This real-world problem was addressed by two distinct regression tasks by using instrumental and sensory measurements. The former is based in the *Warner-Bratzler Shear (WBS)* force, which is an objective measure obtained from a special device called *Instron*. The latter involves the use of subjective information, requiring the execution of a human *Sensory Taste Panel (STP)*. In both cases, the *FSSVM* combination outperformed other *Neural Network (NN)* and *Multiple Regression* configurations.

The final solution is much simpler, requiring only half the number of inputs (6 instead of 12). Moreover, the proposed method is noninvasive, much cheaper than the *WBS* or *STP* procedures, and can be computed just 1 (*STP*) or 24 hours (*WBS*) after slaughter. This opens the room for the development of automatic tools for decision support [19].

One drawback may be the obtained accuracy, which is only 18% (*WBS*) and 12% (*STP*) better than the simple average predictor. However, it should be stressed that the tested datasets are very small. As argued by Lavrač et al. [14], there are important *Data Mining* applications where the data is scarce and more research is needed towards methods that can deal with such datasets. This work backs this claim. Furthermore, Díez et al. [6] considered the modeling of sensory preferences a very difficult regression task. To our knowledge, this is the first time lamb meat quality is approached by *SVMs* and further exploratory research needs to be performed.

Another relevant point regards the input importance. Some results, such as the gender null impact and breed relevance (for the *STP* task), seem to contradict the animal science theory. Regarding the breed importance, the results were discussed with the experts, which then discovered that the *Mirandesa* lambs were considered less stringy and more odor intense, which may be due to animal stress during slaughter. Nevertheless, further research is needed towards this issue.

In future work, the proposed approach will be tested in a real environment, by attaching computer systems with friendly human interfaces into meat laboratories and/or slaughterhouses. This will allow us to obtain, after some time, a valuable feedback from the meat users, and also to enrich the datasets by gathering more meat samples.

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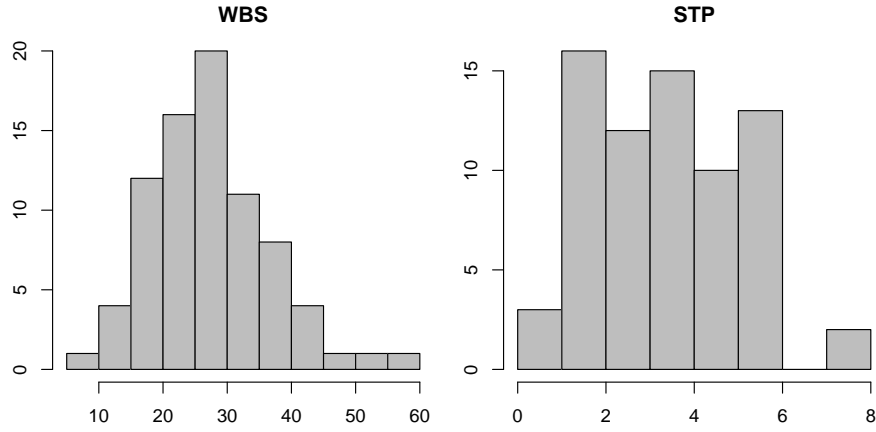


Figure 1. The histograms for the instrumental and sensory output variables

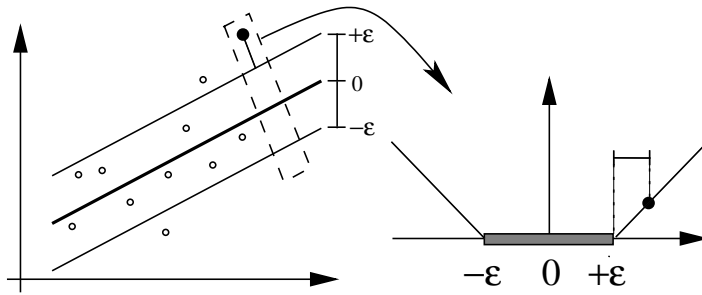


Figure 2. Example of a linear *Support Vector Machine* regression and the ϵ -insensitive loss function (adapted from [18])

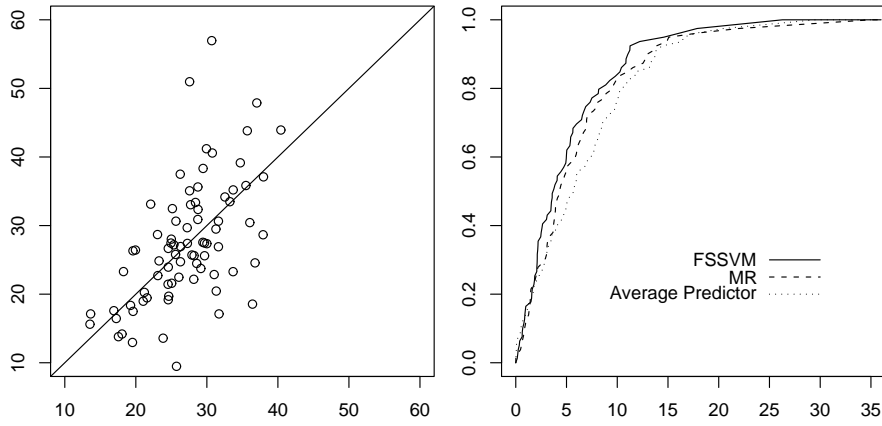


Figure 3. The predicted (x -axis) versus observed (y -axis) values for *FSSVM* (left) and the REC curves (right) for the **WBS** task

Table I. The dataset main attributes

Attribute	Description	Domain
Breed	Breed type	$\{Bragançana, Mirandesa\}$
Sex	Lamb sex	$\{Male, Female\}$
HCW	Hot carcass weight (kg)	$[4.1, 14.8]$
STF2	Sternal fat thickness	$[6.0, 27.8]$
C	Subcutaneous fat depth	$[0.3, 5.1]$
pH1	pH 1 hour after slaughtering	$[5.5, 6.8]$
pH24	pH 24 hours after slaughtering	$[5.5, 5.9]$
a*	Red color index	$[11.5, 22.2]$
b*	Yellow color index	$[6.5, 12.5]$
dE	Total color difference	$[46.5, 60.9]$
dL	Luminosity differential	$[-56, -39]$
dB*	Yellow differential	$[15.3, 22.5]$
WBS	Warner-Bratzler Shear force	$[9.5, 57.0]$
STP	Sensory Taste Panel	$[0.7, 7.1]$

Table II. The regression results

Task	Model	Inputs	Time	MAD	$RMAD$
WBS	MR	12	53	6.22 ± 0.00	91.42 ± 0.00
	NN	12	69869	6.17 ± 0.09	90.56 ± 1.27
	SVM^*	12	28202	5.73 ± 0.04	84.16 ± 0.52
	$FSNN$	6	72698	6.12 ± 0.06	89.94 ± 0.81
	$FSSVM^{\dagger \diamond}$	6	60554	5.60 ± 0.02	82.18 ± 0.33
STP	MR	12	46	1.24 ± 0.00	90.31 ± 0.00
	NN	12	60512	1.35 ± 0.02	98.21 ± 1.19
	SVM^*	12	24536	1.22 ± 0.01	88.48 ± 0.83
	$FSNN^{\dagger}$	6	63345	1.25 ± 0.02	90.91 ± 1.16
	$FSSVM^{\diamond}$	6	52952	1.21 ± 0.01	88.28 ± 0.40

- \star - Statistically significant (p -value < 0.05) under pairwise comparisons with the previous MR and NN models
 \dagger - Statistically significant under a pairwise comparison with the same model without the FS procedure
 \diamond - Statistically significant under a pairwise comparison with $FSNN$

Table III. The relative importance of the input variables (in %)

Task	Model	Attribute								
		Bre.	HCW	STF2	pH1	pH24	a*	dE	dL	dB*
WBS	$FSNN$	0.4	7.4	5.2	0.3	1.3	58.4	20.2	2.9	3.6
	$FSSVM$	0.3	–	25.4	0.4	7.1	32.4	–	19.2	14.9
STP	$FSNN$	35.3	2.7	4.6	12.9	–	25.1	17.5	0.3	0.3
	$FSSVM$	41.3	7.8	0.7	16.0	–	26.3	–	0.3	6.9

